







I  
A BRIEF  
( Yet full )  
ACCOUNT  
OF THE  
DOCTRINE  
OF  
*Vulgar and Decimal*  
FRACTIONS  
WITH A  
Specimen of their Demonstrations.

By WILLIAM ALINGHAM,  
Teacher of the Mathematicks.

L O N D O N,

Printed; Sold by Mr. Mount at the Postern on Tower-Hill,  
Mr. Lea, Globe-maker in Cheapside. Mr. Worgan, Mathe-  
matick-Instrument-maker, under St. Dunstan's Church in  
Fleetstreet; and by the Author, at his House in Channel-  
Row, Westminster, 1698.



---

---

THE  
PREFACE.

Reader,

**T***Hou art here presented with a short  
Treatise of Vulgar and Deci-  
mal Fractions, Quantities of such  
great and general Use, that without the  
Knowledge of them there can be no Com-  
pleat, or Correct Accomptant.*

*I have therefore in this Critical Age  
adventnr'd to present the Publick with  
this small Tract, in which I have en-  
deavoured to be Methodical and Plain,  
and to digest the Rules in such Order,  
with several Exemplications of the same,  
that*



## The Preface.

*that I hope they will be rendered intelligible, and serviceable to the meanest Capacity.*

*Lastly, I have added a Specimen of the Demonstration of each particular Operation: All which to the Ingenious I willingly present, hoping of their favourable Acceptance; and that they may receive some Benefit from the same, is the hearty Wish of their real Friend*

W. Alingham.

---

THE



---



---

T H E  
DOCTRINE  
O F  
Vulgar Fractions.

*What a Fraction is, and how read.*

**A**N Unite, or Integer, is one whole thing, as, one Pound, one Yard, one Gallon, one Hour, &c.

A Fraction, or broken Number, is a part, (or parts) of an Unite, or Integer; and is generally represented by two Numbers set one over the other, with a Line between them, thus,  $\frac{1}{2} \cdot \frac{2}{3} \cdot \frac{3}{4} \cdot \frac{5}{7}$ , &c. The upper number is termed the Numerator; the lower the Denominator; they are read, or pronounced, thus,  $\frac{1}{2}$  is one half,  $\frac{2}{3}$  is two thirds,  $\frac{3}{4}$  is three fourths,  $\frac{5}{7}$  is five sevenths, and so of any other, naming the Numerator first, and the Denominator last; the Denominator

B shewing

shewing the parts into which the Unite, or Integer, is broke, and the Numerator, the part, ( or parts ) of the Denominator that is to be taken, or used.

*Of the Varieties of Fractions.*

**O**F *Fractions*, or broken Numbers, there are four sorts, viz. *Proper*, *Improper*, *Mixt* and *Compound*.

A *proper Fraction* is, that whose Numerator is lesser than the Denominator, as  $\frac{1}{2} \cdot \frac{2}{3} \cdot \frac{3}{4} \cdot \frac{4}{5} \cdot \&c.$

An *Improper Fraction*, is, that whose Numerator is greater than ( or, at least equal to ) the Denominator, as  $\frac{4}{3} \cdot \frac{5}{2} \cdot \frac{6}{8} \cdot \frac{4}{4} \cdot \&c.$

*Mixt*, are whole Numbers and Fractions set together thus,  $2\frac{1}{3}$ ,  $3\frac{5}{8}$ ,  $7\frac{3}{4}$ , &c.

*Compound Fractions* are known, by having the word [ *Of* ] betwixt them, and are written thus,  $\frac{2}{3}$  of  $\frac{3}{4}$ , also  $\frac{1}{4}$  of  $\frac{5}{8}$  of  $\frac{7}{8}$ . They are likewise called Fractions of Fractions.

Now before we can pass to the Rules of *Addition*, *Substraction*, *Multiplication* and *Division* in Fractions, they must be prepar'd, and made fit for such Operation, and this preparation is perform'd by *Reduction*, of which there are five kinds, as follows,

*Reduction*



*Reduction the First.*

**T**eacheth how to reduce a whole, or mixt Number, into an *Improper Fraction*, which Fraction shall be equal in value to the said whole, or mixt Number : And contrary, that is, it teacheth to turn an improper Fraction into its Equivalent whole, or mixt Number.

*CASE I.* If it be a whole Number, the Rule is, multiply it by the assign'd Denominator, setting the Product thereof for a Numerator over the said Denominator, so shall this Fraction be equal to the given whole Number.

*Example.* Reduce 7 into an Improper Fraction, whose Denominator shall be 4.

7 whole Number,

4 assign'd Denom. So that  $7 = \frac{28}{4}$ .

28 Numerator requir'd.

*Note,* That these two Lines  $=$  is the sign of Equality, as  $7 = \frac{28}{4}$  shows that 7 is equal to 28 Fourths.

*More Examples.*

Reduce  $\left\{ \begin{array}{l} 5 \\ 8 \\ 9 \end{array} \right\}$  into a Fraction,  $\left\{ \begin{array}{l} 4 \\ 6 \\ 7 \end{array} \right\}$  whose Denom. is

B 2

CASE

*CASE 2.* If a mixt Number is given to be reduc'd, the Rule is, multiply the whole Number by the Denominator of the Fraction, adding thereto its Numerator, the Sum shall be a new Numerator which, if set over the old Denominator will give a Fraction of the same value with the propos'd mixt Number.

*Exam.* Reduce  $2\frac{3}{4}$  into an Improper Fraction.

$$2\frac{3}{4}$$

4 Denom.

$$\text{So that } 2\frac{3}{4} = \frac{11}{4}.$$

11 new Numer.

*More Examples.*

Reduce  $\left\{ \begin{array}{l} 3\frac{5}{7} \\ 6\frac{2}{3} \\ 5\frac{4}{9} \end{array} \right\}$  into an Improper Fraction.

*CASE 3.* If an Improper Fraction is to be reduced into its Equivalent whole, or mixt Number; the Rule is, divide the Numerator by the Denominator, so will the Quotient give a whole Number equal to the Fraction given.

*Exam.* Reduce  $\frac{28}{4}$  into its Equivalent whole Number.

$$4 \overline{) 28} \quad (7 \text{ the whole Number requir'd.}$$

$$28$$

$$\overline{28}$$

$$00$$

$$\text{So that } \frac{28}{4} = 7.$$

*More*



*More Examples.*

Reduce  $\left\{ \begin{array}{l} \frac{20}{4} \\ \frac{48}{6} \\ \frac{62}{7} \end{array} \right\}$  into its Equivalent whole Numb.

---

If after dividing any thing remain, set it for a Numerator over the Fractions Denominator, and join the said Fraction to the Quotient.

*Exam.* Reduce  $2\frac{1}{4}$  into its Equivalent mixt Number.

$$\begin{array}{r} 4 \overline{) 11} \quad (2\frac{3}{4} \text{ mixt Numb.} \\ \underline{8} \\ 3 \end{array}$$

*More Examples.*

Reduce  $\left\{ \begin{array}{l} \frac{26}{7} \\ \frac{20}{3} \\ \frac{49}{9} \end{array} \right\}$  into its Equivalent mixt Numb.

*This Reduction is absolutely necessary, for there is no working with whole Numbers and Fractions, till the whole Numbers are turn'd into Fractions.*

*Reduction the Second,*

**T**Eacheth you how to reduce a compound Fraction to a Simple one, which shall have the same value with it.

B 3

RULE.

## R U L E.

Multiply all the Denominators one into another continually, and set the Product thereof for a Denominator; so likewise multiply all the Numerators one into another, and set the Product for a Numerator over the former Denominator, the Fraction thus form'd is Equivalent to the given compound Fraction.

*Example,*

Reduce  $\frac{3}{4}$  of  $\frac{8}{9}$  of  $\frac{2}{12}$  to a simple Fraction.

3 Numer. 1st.

4 Den. 1st.

8 Numer. 2d.

9 Den. 2d.

---

24

---

36

9 Numer. 3d.

12 Den. 3d.

---

216 Numer. sought      432 Den. sought.

So that  $\frac{3}{4}$  of  $\frac{8}{9}$  of  $\frac{2}{12} = \frac{216}{432}$ .

Reduce  $\left\{ \begin{array}{l} \frac{4}{5} \text{ of } \frac{5}{6} \text{ of } \frac{8}{9} \\ \frac{3}{6} \text{ of } \frac{6}{7} \text{ of } \frac{7}{9} \\ \frac{3}{5} \text{ of } \frac{7}{8} \text{ of } \frac{10}{12} \end{array} \right\}$  to a simple Fraction

*This Reduction is likewise absolutely necessary, for there is no working with Compound Fractions, and others, till the said Compounds are reduc'd to Simple.*

*Redu.*



*Reduction the Third.*

**T**Eacheth how to abbreviate a Fraction, or to find a Number that shall reduce it to its lowest Terms at one Operation, yet still keeping the same value it had at first.

*RULE* 1<sup>st</sup>.

Divide the Numerator and Denominator ( if they be both even ) by 2. 4. 6. 8. &c. ( If the Numerator and Denominator be one even, and the other odd, then try some odd Number, as 3. 5. 7. 9. &c.) that will divide both without a remainder ; repeat this Division as often as you can, so shall the last Quotient of the Numerator be a new Numerator, and the last Quotient of the Denominator, a new Denominator.

*Example.*

Reduce  $\frac{216}{432}$  into its lowest Terms.

$$\frac{216}{432} \bigg| \frac{2}{108} \bigg| \frac{3}{36} \bigg| \frac{9}{4} \bigg| \frac{1}{2} \quad \text{So that } \frac{216}{432} = \frac{1}{2}.$$

*More Examples.*

Reduce  $\left\{ \begin{array}{r} 160 \\ 270 \\ 216 \\ 378 \\ 2240 \\ 3300 \end{array} \right\}$  into its lowest Terms.

But

But the general way of reducing a Fraction to its lowest Terms, is, to find a Common Measurer, that is, the greatest number, which will divide the Numerator and Denominator without a Remainder, by which means a Fraction is brought to its lowest terms at the first work: For finding of which the Rule is;

*RULE* 2d.

Divide the Denominator by the Numerator, and if any thing remain by it, divide the former Divisor, and if after this division any thing remain, divide the last divisor by it: *Proceed* thus till nothing remain, so shall the last Divisor be the greatest common Measurer, and is a Number that will divide both Numerator and Denominator without a Remainder, and so reduce the Fraction to its lowest terms at one Operation: But, if after all the Divisions are ended there remains one, then is such Fraction in its lowest terms already.

*Exam.* Reduce  $\frac{2\frac{1}{4}}{\frac{3}{2}}$  to its lowest Terms.

216 ) 432 ( 2

432

—

∴

So



So that 216 is the common Measurer, and is the greatest Number that will divide the Numerator and Denominator without a Remainder. See the work

$$216) \frac{2\frac{1}{3}\frac{6}{2}}{4\frac{1}{3}\frac{6}{2}} (\frac{1}{2} \text{ the Fraction sought.}$$

After this method you may try the Examples given, in the first Rule of this Reduction.

*This Reduction is also very useful, for by it Fractions that are express'd by great Numbers, are made to be express'd by smaller, so that their true value is more easily and readily known.*

### *Reduction the Fourth.*

**T**Eacheth how to bring Fractions of divers denominations into Fractions of one denomination, yet still retaining the same value.

#### *RULE.*

Multiply all the Denominators continually one into another, and set the product thereof for a new Denominator; then multiply the Numerator of the first Fraction into all the Denominators, except its own, the product is the Numerator of the first Fraction, and must be

C

set

set over the Denominator before found. So likewise for the second Fraction you must multiply its Numerator into all the Denominators, except its own, the product is the Numerator of the second Fraction. *Proceed* thus with the rest of the Numerators, *that is*, Multiply each Numerator by all the Denominators, except its own, setting the several Products for new Numerators over the common Denominator first found, so shall these new Fractions be of one denomination, and equivalent to the former.

*Example.*

Reduce  $\frac{2}{3}$  and  $\frac{4}{7}$  and  $\frac{5}{8}$  into one Denomination.

3 Denom. 1st.

7 Denom. 2d.

---

21

6 Denom. 3d.

---

126 Common Den.

4 Numer. 2d.

3 Denom. 1st.

---

12

6 Denom. 3d.

---

72 New Numer. 2d.

2 Numer. 1st.

7 Denom. 2d.

---

14

6 Denom. 3d.

---

84 New Numer. 1st.

5 Numer. 3d.

7 Denom. 2d.

---

35

3 Denom. 3d.

---

105 New Numer. 3d.

So



So that  $\left\{ \begin{array}{l} \frac{2}{3} = \frac{84}{126} \\ \frac{4}{7} = \frac{72}{126} \\ \frac{5}{8} = \frac{105}{126} \end{array} \right\}$

*More Example.*

Reduce  $\left\{ \begin{array}{l} \frac{2}{5} \& \frac{1}{7} \& \frac{5}{8} \\ \frac{3}{7} \& \frac{1}{2} \& \frac{5}{8} \\ \frac{3}{2} \& \frac{1}{5} \& \frac{7}{9} \end{array} \right\}$  into one denomination

*Note 1st.*

If mixt Numbers are given thus to be reduc'd, reduce only the fractional parts.

*Note 2d.*

If compound Fractions are to be reduc'd to one Denomination, they must first be brought to simple ones by *Reduction the Second*.

*This Reduction is also highly necessary, for before Fractions are brought to the same Denomination, they neither can be Added, nor Subtracted.*

*Reduction the Fifth.*

**T**Eacheth how to alter, or change, a Fraction into another equal in value that shall have any assign'd Denominator.

C 2

*RULE.*

## RULE.

Multiply the Numerator of the Fraction by the assign'd Denominator, and divide the Product by the old Denominator, the Quotient is the Numerator to the intended Denominator.

*Example.*

Reduce  $\frac{84}{126}$  into a Fraction, whose Denominator shall be 3.

84 Numer.

3 Denom. assign'd.

$$\begin{array}{r} \text{So that } \frac{84}{126} = \frac{2}{3}. \\ 126 \overline{) 252} \quad (2 \text{ the new Num.} \\ \underline{252} \\ \dots \end{array}$$

*More Examples.*

Reduce  $\left\{ \begin{array}{l} \frac{84}{210} \\ \frac{48}{112} \\ \frac{135}{360} \end{array} \right\}$  into a Fraction  $\left\{ \begin{array}{l} 5 \\ 7 \\ 8 \end{array} \right\}$  for a Den.

*Note,* If a compound Fraction is thus to be reduc'd, then by *Reduction* 2d. turn it to a simple, and then work as the preceding Rule directs.

*How to find the value of a Fraction.*

This Reduction is the most useful of all others, for by it the value of any Fra-



Fraction is found in the known parts of Coyn, Weight, Time, &c. *And contrary, that is,* any part of Coyn, Weight, Time, &c. is turn'd into a Fraction; the method of doing which is as follows,

Multiply the Numerator by the parts of the next inferior Denominator, that are equal to an Unite of the same, that the Fraction gives the parts of; the Product divide by the Denominator, the Quote gives the value in the parts you multiply'd by: If after this Division any thing remain, multiply it by the next inferior Denomination, dividing the Product by the Denominator, as before. *Thus proceed,* till you can bring it no lower, so will the several Quotients give the required value of the given Fraction.

*Example 1st.*

*What's the  $\frac{6}{8}$  of a Shilling.*

$$\begin{array}{r} 6 \\ 12 \\ \hline 8 \overline{) 72} (9 \text{ So that } 9 \text{ d. is the } \frac{6}{8} \text{ of a Shill.} \\ 72 \\ \hline \end{array}$$

But if when it be brought to the lowest Terms any thing remain, place it  
C 3 for

( 14 )

for a Numerator over the former Denominator.

*Example 2d.*

*What's the  $\frac{17}{9}$  of a Pound sterling.*

$$\begin{array}{r} 17 \\ 20 \\ \hline 19 \overline{) 340} \text{ (17 Shill. } 17 \text{ the 1st Remainder} \\ 19 \\ \hline 150 \\ 133 \\ \hline 17 \\ \hline 14 \text{ the 2d. Remainder.} \\ 4 \\ \hline 19 \overline{) 56} \text{ ( 2 Far.} \\ 38 \\ \hline 18 \text{ the 3d. Remainder.} \end{array}$$

So that  $\frac{17}{9}$  of a Pound is 17 s. 10 d.  $\frac{1}{2}$  and  $\frac{18}{9}$  of a Fathing.

*Example 3d.*

*What's the  $\frac{5}{9}$  of a Pound weight, Averdupoize.*



8 Remain.

16

5 Num.

16

9 ) 128 ( 14 Drums.

9

9 ) 80 ( 8 Oun.

72

9 ) 38

36

8

2

So that  $\frac{5}{9}$  of a Pound weight Averdupoize, is 8 Ounces 14 Drums  $\frac{2}{9}$ .

After this method may the value of any Fraction be found ( whether it be of *Coyne, Weight, Time, Liquor Measure, Long Measure, &c.* ) and given in known and familiar Terms, as in the second Example, where the value of  $\frac{17}{9}$  of a Pound sterling was required. I answer, that it is 17 Shillings 10 Pence Half-penny, and  $\frac{1}{9}$  of a Farthing. So likewise in the third Example, where the  $\frac{5}{9}$  of a pound weight Averdupoize was required ; there I answer, that it was 8 Ounces, 14 Drums, and  $\frac{2}{9}$  of a Dram.

How



*How to turn any part of Coyn, Time,  
Weight, &c. into a Fraction.*

**T**His is but the Converse of the former, and therefore ( from a little consideration of what foregoes ) may be easily effected : For if you do but consider that 1 Shilling is the  $\frac{1}{20}$  of a Pound sterling, and 1 Penny the  $\frac{1}{12}$  of a Shilling, and 1 Farthing the  $\frac{1}{4}$  of a Penny : The Names of a Shilling, a Penny, and a Farthing, being only Denominations given them, for the Vulgar in our Nation to know them by, the more universal way of expressing them, being to call a Shilling the  $\frac{1}{20}$  of a Pound, and a Penny the  $\frac{1}{12}$  of a Shilling, also a Farthing the  $\frac{1}{4}$  of a Penny : And this way of expressing them ( supposing the value of the Pound known ) would be intelligable to all Nations that have the knowledge of Numbers ; so that if it were requir'd to know what part of a Shilling 9 d. is, I answer, that 'tis  $\frac{9}{20}$ , or when abbreviated  $\frac{3}{4}$ . In like manner, if it were required to know what part of a pound 4 Shillings, it is evident that 'tis  $\frac{4}{20}$  or  $\frac{1}{5}$ . But if it were requir'd to know what part of a Pound 1 Penny is, here I must  
con,

consider that 1 Penny is the  $\frac{1}{12}$  of  $\frac{1}{20}$  of a Pound, and therefore if by *Reduction* the 2d. I reduce it to a simple Fraction, 'twill be  $\frac{1}{240}$  of a pound Sterling, so a Farthing is  $\frac{1}{4}$  of  $\frac{1}{12}$  of  $\frac{1}{20}$  of a pound, and therefore the  $\frac{1}{960}$  of a pound: Lastly, if it be required to know what part of a Pound 13 s. 5 d.  $\frac{1}{4}$  is, then reducing all into Farthings, it gives 645 ; and likewise finding the Farthings in one pound which is 960, and setting the former over the latter fraction-wise gives  $\frac{645}{960}$ , the part of a pound that 13 s. 5 d.  $\frac{1}{4}$  is.

After the same manner may any part of Weight, Time, Measure, &c. be expressed Fraction-wise.

*Some Examples, with their Answers.*

What's the  $\frac{1}{4}$  of a Pound sterling.

*Answer,* 18 s. 6 d.  $\frac{3}{4}$  q.  $\frac{3}{7}$ .

What's the  $\frac{6}{7}$  of a Guinea at 22 s.

*Answer,* 15 s. 8 d.  $\frac{1}{2}$  q.  $\frac{2}{7}$ .

What's the  $\frac{3}{8}$  of a Pistole at 17 s. 10 d.

*Answer,* 6 s. 8 d.  $\frac{1}{4}$ .

What's the  $\frac{2}{9}$  of a pound Weight Averdupoize. *Answer,* 3 Oun. 8 Dr.  $\frac{8}{9}$ .

What's the  $\frac{6}{7}$  of a Year, at 365 days.

*Answer,* 312 days, 20 hours, 34 min.  $\frac{2}{7}$ .

What part of a Pound sterling is 2 s. 9 d.

*Answer,*  $\frac{23}{240}$ .

D

What



( 10 )  
What part of a pound Averdupoize is  
11 Ounces 2 Drams  $\frac{1}{4}$ . Answer  $\frac{713}{1014}$ .

What part of a Year is 29 days, 14  
hours. Answer,  $\frac{713}{8780}$ .

The reason of this Reduction is very evident, for in a given Fraction suppose  $\frac{2}{3}$ , such proportion as the Denominator 3 has to its Numerator 2. such proportion has any assign'd Denominator, suppose 6, to a Numerator corresponding to it, so that stating the Question according to the Rule of Three, viz. If 3 give 2, what shall 6 give, and then as is directed multiplying the second term 2, which is the Numerator, by the third term 6 the assign'd Denominator, dividing the product by the first term 3 the old Denominator, you get 4 for the Quotient, which is a new Numerator to the assign'd Denominator.

'Tis by this Reduction we turn a Vulgar Fraction to a Decimal, & contra, also by it all the Decimal Tables are calculated, of which more shall be said when I come to treat of Decimals.

### *Addition of Vulgar Fractions.*

**I**F the Fractions to be added have not like Denominators, they must be reduc'd to a common Denominator by Reduction



duction the 4th. Then add the Numerators together, and set the Summ for a Numerator over the common Denominator, so shall the Fraction thus found be the Summ of the given Fractions.

*Example.*

What's the Summ of  $\frac{2}{3}$  and  $\frac{5}{7}$ .

Reduc'd to a common Denom.  $\left\{ \begin{array}{l} \frac{14}{21} \\ \frac{15}{21} \end{array} \right.$   
they stand thus,  $\frac{14}{21} + \frac{15}{21}$

the Summ  $\frac{29}{21}$  or  $1\frac{8}{21}$ .

Observe if the Fraction that is the Summ of those two given, happen to be an Improper Fraction, then by Reduction the 1st. Rule the 3d. reduce it into its equivalent whole, or mixt Number as in the last *Exam.*

*More Examples.*

What's the Summ of  $\left\{ \begin{array}{l} \frac{2}{5} \\ \frac{4}{9} \end{array} \right.$

What's the Summ of  $\left\{ \begin{array}{l} \frac{4}{7} \\ \frac{6}{9} \\ \frac{2}{5} \end{array} \right.$

*Note 1.*

If you are to add mixt Numbers, add only the fractional parts, being first reduc'd to a common Denominator by Reduction the 4th.

D 2

*Note*

*Note 2.*

If compound Fractions are to be added one to another, or to simple Fractions, then such Compound Fractions must be reduc'd to simple ones ( by Reduction the 2d. ) and those again to one Denomination by Reduction the 4th.

*Note 3.*

If the Fractions to be added are not parts of the same whole, but the one parts of a Shilling, the other of a Pound, then ( by Reduction the 5th. ) they must be brought to one Name, or Denomination, *i. e.* both must be made parts of the same whole.

*As for Example.*

What's the Summ of  $\frac{3}{5}$  of a Pound, and  $\frac{2}{3}$  of a Shilling.

Here they are not only of different denominations, but parts of different Wholes, and therefore is more properly worded thus,

What's the Summ of  $\frac{3}{5}$  and  $\frac{2}{3}$  of  $\frac{1}{20}$  of a Pound sterling. *Answer,*  $\frac{120}{3000}$ .

*Substraction*



## *Subtraction of Vulgar Fractions.*

**T**HE Rules delivered for reducing and making Fractions fit for Addition, are in all respects and cases to be observ'd in Subtraction; so that whether they are Mixt, Compound, or simple ones, they must be reduc'd to a common Denominator; then take the Numerator of the Subtractor, or Fraction, to be Subtracted, from the Numerator of the Subtrahend ( or Fraction from which we are to Subtract ) and set the remainder over the common Denominator, so is this new Fraction the remainder or difference sought.

### *Example.*

From  $1\frac{8}{21}$  or  $\frac{22}{21}$  subtract  $\frac{2}{3}$ .

Reduc'd to a common Denom.  $\left\{ \begin{array}{l} \frac{87}{63} \\ \frac{42}{63} \end{array} \right.$   
they stand thus,  $\frac{\quad}{63}$

Remainder  $\frac{45}{63}$  or  $\frac{5}{7}$ .

### *More Examples.*

From  $\frac{38}{45}$  Subtract  $\frac{4}{9}$ .

From  $\frac{201}{315}$  Subtract  $\frac{3}{5}$ .

D 3

*Multi*

## *Multiplication of Vulgar Fractions.*

**I**F they be simple Fractions to be Multiply'd. Then Multiply the two Numerators, together, for a Numerator, and the two Denominators for a Denominator, so shall the Fraction formed by these two Numbers be the product Required.

*Example.*

Multiply  $\frac{5}{4}$  by  $\frac{8}{5}$ .

$$\begin{array}{r} 5 \} \text{Numerators.} \quad 8 \} \\ 4 \} \quad \quad \quad 5 \} \text{Denominators.} \\ \hline 20 \quad \quad \quad 40 \end{array}$$

So that  $\frac{20}{40}$  or  $\frac{1}{2}$  is the Product requir'd.

*More Examples*

Multiply  $\frac{7}{9}$  by  $\frac{8}{11}$ .

Multiply  $\frac{5}{6}$  by  $\frac{2}{7}$ .

Multiply  $\frac{4}{5}$  by  $\frac{3}{4}$ .

*Note 1st.*

If mixt Numbers are to be Multiply'd then before you can Multiply them they must be Reduc'd into Improper Fractions by Reduction the 1<sup>st</sup>. Rule the 1<sup>st</sup>. and 2<sup>d</sup>.

*Note*



*Note 2d.*

If they be Compound Fractions, Reduce them to simple ones.

*Note 3d.*

If a whole Number is to be Multiplied by a Fraction, then make the whole Number an Improper Fraction by setting one under it.

### *Division of Vulgar Fractions.*

**I**F the Fraction to be divided, and also the Fraction by which we divide, *that is*, Dividend and Divisor, be both simple Fractions, then Multiply the Numerator of the Dividend by the Denominator of the Divisor, and set the product for a Numerator; multiply also the Denominator of the Dividend, by the Numerator of the Divisor, and take the product for a Denominator; the Fraction thus form'd is the Quotient.

*Example.*

Divide  $\frac{2}{4}$  by  $\frac{4}{5}$ .

$\frac{4}{5}) \frac{2}{4} (\frac{1}{8}$  or  $\frac{1}{8}$  the Quotient.

*More*

*More Examples.*

Divide  $\frac{5}{9}\frac{6}{9}$  by  $\frac{2}{9}$ .

Divide  $\frac{1}{4}\frac{0}{2}$  by  $\frac{2}{7}$ .

Divide  $\frac{1}{2}\frac{2}{5}$  by  $\frac{4}{5}$ .

*Note 1st.*

If either Dividend, Divisor or both, be whole or mixt Numbers, reduce them into Improper Fractions, by Reduction the 1st. Rule 1st. or 2d. and then divide according to the preceding Rule.

*Note 2d.*

If they be Compound Fractions reduce them to simple ones by Reduction the 2d.

*The Rule of Three Direct in Fractions.*

**T**HE Directions given, both for stating and working Questions in the Rule of Three in whole Numbers, holds also in this of Fractions; so that having framed your Question, as is there directed, 'tis but Multiplying the Fractions in the 2d. and 3d. place together, and divided the product by the first, according  
to



to the preceding Rules given for Multiplying and dividing of Fractions, the Quotient is the Answer to the Question.

*Example.*

If  $\frac{2}{3}$  of a Yard of Cloath cost  $\frac{1}{7}$  of a Pound, what Cost  $\frac{7}{8}$  of a Yard at that Rate.

$$\text{If } \frac{2}{3} \text{ ————— } \frac{1}{7} \text{ ————— } \frac{7}{8}$$

$$\frac{2}{3}) \frac{35}{58} \left( \frac{105}{112} \text{ of a Pound for Answer.}$$

*Proof.*

$$\text{If } \frac{7}{8} \text{ ————— } \frac{105}{112} \text{ ————— } \frac{2}{3}$$

$$\frac{7}{8}) \frac{210}{336} \left( \frac{1680}{2352} \text{ or } \frac{5}{7}.$$

*More Examples.*

If  $\frac{8}{9}$  of a pound Troy cost  $\frac{5}{7}$  of a Guinea, at 22 s. What shall  $\frac{2}{11}$  of a pound cost. *Answer*  $\frac{405}{818}$ . or 14 s. 5 d.  $\frac{1}{2}$   $\frac{2}{7}$ .

If  $\frac{4}{5}$  of a pound Troy cost  $\frac{3}{7}$  of a Noble, What will  $\frac{14}{15}$  of a Noble buy. *Answer* .  $\frac{392}{225}$  or 1 pound  $\frac{167}{225}$ .

If  $\frac{1}{12}$  of an Hundred weight cost 34 s.  $\frac{3}{4}$ , What will 19 Hundred weight  $\frac{3}{4}$  cost. *Answer*  $\frac{413144}{392}$  or 1155  $\frac{384}{392}$ .

*Note 1.* If there be mixt Numbers, reduce them to Improper Fractions.

E

*Note*

*Note 2.* If any of the given Fractions be Compound, that is Fractions of Fractions, they must be reduc'd to simple Fractions by Reduction the 2d.

*The Rule of Three Reverse in Fractions.*

**H**ere also, as in that of whole Numbers, you are to Multiply the second Term by the first, and divide the product by the third, the Quotient answers the Question.

*Example.*

If  $\frac{2}{3}$  of a Yard of Cloath that is a yard broad will make a Garment, How much of 3 Yards wide will make the said Garment.

$$\text{If } 1 \text{ Yard } \text{---} \frac{2}{3} \text{---} \text{---} 3 \\ \frac{1}{1} \text{ by } \frac{2}{3} = \frac{2}{3} \quad \frac{3}{1} ) \frac{2}{3} ( \frac{2}{9} \text{ for Answer.}$$

*Proof.*

$$\text{If } 3 \text{---} \frac{2}{9} \text{---} \text{---} 1 \\ \frac{3}{1} \text{ by } \frac{2}{9} = \frac{6}{9} \\ \frac{1}{1} ) \frac{6}{9} ( \frac{6}{9} = \frac{2}{3}.$$

*More Examples.*

If 54 Men can build a House in 38 days  $\frac{2}{3}$ , How many Men will build the said House in 11 days  $\frac{5}{8}$ . *Answer* 176 Men  $\frac{2}{3} \frac{5}{8}$ . Lent



( 27 )  
Lent my Friend  $\frac{5}{8}$  of a pound for  $\frac{2}{3}$  of a Year, How much ought he to lend me for 2 Years, to recompence my kindness.

*Answer*  $\frac{5}{24}$ .

If when a Bushel of Wheat is sold for 5 shillings  $\frac{2}{3}$ , the penny white Loaf weighs 7 Ounces  $\frac{3}{4}$ , What must it weigh when the Bushel of Wheat cost 6 shillings  $\frac{4}{7}$ .

*Answer*, 6 Ounces  $\frac{377}{552}$ .

---

*A Collection of pleasant and useful Questions to Exercise the Rules of Vulgar Fractions,*

*By Reduction 5th.*

**W**hat's the  $\frac{2}{3}$  of 17 s. *Answer* 11 s. 4 d.

What's the  $\frac{5}{7}$  of  $\frac{2}{5}$  of a Guinea at 21 s. 2 d. *Answer*, 6 s. 00 d.  $\frac{1}{2}$  q.  $\frac{2}{7}$ .

What's the  $\frac{2}{3}$  of half a Mark. *Answer* 4 s. 5 d.  $\frac{1}{4}$  q.  $\frac{1}{3}$ .

What's the  $\frac{3}{5}$  of a Dollar at 4 s. 2 d. *Answer*, 2 s. 6 d.

What's the  $\frac{7}{9}$  of 5 pounds. *Answer*, 3 l. 17 s. 9 d.  $\frac{1}{4}$  q.  $\frac{1}{3}$ .

What's the  $\frac{5}{8}$  of 13 d.  $\frac{1}{2}$ . *Answer* 8 d.  $\frac{1}{4}$  q.  $\frac{3}{4}$ .

What's the  $\frac{3}{7}$  of 8 Ounces  $\frac{1}{2}$  Troy weight. *Answer* 3 oz. 12 dwt. 20 gr.  $\frac{4}{7}$ .

What's the  $\frac{7}{9}$  of 15 days 3 hours. *Answer*, 11 days 18 hours 20 minutes.

*By Reduction 2d. and 5th.*

What's the  $\frac{1}{2}$  of  $\frac{2}{3}$  of a pistole at 18 s. *Answer*, 6 s.

What's the  $\frac{5}{7}$  of  $\frac{8}{9}$  of a Ducat at 7 s. 3 d. *Answer* 4 s. 7 d. 0 q.  $\frac{2}{11}$ .

What's the  $\frac{3}{4}$  of  $\frac{1}{8}$  of  $\frac{7}{8}$  of a Guinea at 22 s. 2 d. *Answer*, 12 s. 1 d.  $\frac{1}{4}$  q.  $\frac{7}{8}$ .

What's the  $\frac{3}{8}$  of  $\frac{1}{5}$  of 13 l. 4 s. 7 d. *Answer* 19 s. 10 d. 0 q.  $\frac{1}{8}$ .

What's the  $\frac{2}{3}$  of  $\frac{3}{4}$  of 5 Nobles. *Answer* 16 s. 8 d.

What's the  $\frac{2}{5}$  of  $\frac{1}{2}$  of  $\frac{1}{4}$  of 1 lib. 3 oz. 2 dwt. Troy. *Answer*, 15 dwt. 2 gr.  $\frac{2}{5}$ .

*Questions that Exercise most of the preceding Rules.*

**H**OW much is  $\frac{2}{3}$  of  $\frac{1}{8}$  and  $\frac{3}{4}$  of  $\frac{1}{2}$  of a Jacobus at 25 s. *Answer* 1 l. 3 s. 3 d. 0 q.  $\frac{2}{3}$ .

How much is  $\frac{1}{2}$  of  $\frac{2}{3}$  and  $\frac{7}{8}$  of  $\frac{2}{9}$  of a Hundred weight Averdupoize. *Answer*, 1 c. 0 q. 13 lib.  $\frac{8}{15}$ . What



What Quantity is that, from which if I take  $3\frac{5}{7}$  the remainder shall be  $1\frac{2}{5}$ . *Answer*,  $5\frac{4}{35}$ .

What Quantity is that. from which if I take  $\frac{1}{2}$  of  $\frac{5}{9}$  the remainder shall be  $\frac{2}{7}$  of 5. *Answer*,  $1\frac{89}{126}$ .

What's the difference betwixt  $\frac{1}{2}$ ,  $\frac{1}{3}$  and  $\frac{1}{4}$ , and a whole Unite. *Answer*,  $\frac{1}{12}$ .

What Quantity is that, to which if I add  $3\frac{5}{7}$  the Summ will be  $5\frac{4}{35}$ . *Answer*  $1\frac{2}{5}$ .

What Quantity is that, to which if I add  $\frac{1}{5}$  of  $\frac{2}{7}$ , the Summ will be  $1\frac{89}{126}$ . *Answer*  $\frac{1681}{4410}$ .

A person has  $\frac{2}{7}$  and  $\frac{1}{11}$  of a Mine, What part is that of the whole. *Answer*,  $\frac{22}{77}$ .

Another Miner has  $\frac{3}{4}$  and  $\frac{1}{7}$  and  $\frac{1}{10}$  of a Mine, What share or part is that of the whole. *Answer*  $\frac{107}{112}$ .

A Merchant has  $\frac{3}{10}$  and  $\frac{1}{2}$  of  $\frac{1}{4}$  of a share in the Cargo of a ship, What part is that of the whole. *Answer*  $\frac{40}{128}$ . or  $\frac{5}{16}$ .

Another person has  $\frac{1}{5}$  of  $\frac{1}{8}$  and  $\frac{1}{11}$  of  $\frac{2}{3}$  of a ship, how much is that of the whole. *Answer*,  $\frac{113}{320}$ .

Such Questions as the four last, are frequent among those that have parts in Mines, or Ships.

What's

What's the product of 3 s. 6 d. by 3 s. 6 d. Here you are to consider that 6 d. is a part of a Shilling, and therefore the Question more rightly propos'd is, What's the product of  $3\frac{1}{2}$  by  $3\frac{1}{2}$ . Answer  $4\frac{3}{4}$  or 12  $\frac{3}{4}$  that is 12 s. 3 d.

Again, What's the product of 3 l. 19 s. 11 d. by 3 l. 19 s. 11 d. Here (as before) consider, that 19 s. 11 d. is  $\frac{239}{240}$  of a Pound sterling: And so the Question more rightly stated is, What's the product of  $3\frac{239}{240}$  by  $3\frac{239}{240}$ . Answer,  $\frac{219681}{57600}$  or 15 l. &  $\frac{5681}{57600}$  of a pound.

A certain Person having  $\frac{3}{5}$  parts of a Coal Mine, sells  $\frac{3}{4}$  of his share for 171 l. What is the whole Coal Mine worth. Answer, 380 l.

A Father dying left his Son a certain portion, of which he spent  $\frac{1}{4}$ ; then of the rest he spent  $\frac{1}{2}$ , and then he had 252 l. What was the Portion the Father gave him. Answer, 672 l.

When the  $\frac{2}{5}$  of  $\frac{3}{4}$  of a ship is 147 l. 11 s. 3 d. How much is the whole. Answer, 491 l. 17 s. 6 d.

A Merchant bought  $\frac{2}{3}$  of  $\frac{3}{4}$  of a ship, another buys  $\frac{3}{8}$  of  $\frac{4}{5}$  of the same, the Question is, Whether their parts were equal, and if not, which had the biggest



gest of the two. *Answer*, the first Merchant by  $\frac{1}{5}$ .

A younger Brother received 210 *l.* which was  $\frac{3}{8}$  of  $\frac{2}{3}$  of his Elder Brother's Portion: Now  $3\frac{1}{2}$  times his Elder Brother's Portion was  $1\frac{1}{3}$  time his Father's Estate, I demand what his Father's Estate was. *Answer*, 2205 *l.*

A Person making his Will gave to one Child  $\frac{2}{5}$  of  $\frac{3}{4}$  of his Estate, and to another  $\frac{5}{8}$  of  $\frac{2}{3}$  of his Estate, and when they counted their Portions, the one had 543 *l.* 1 *s.* 9 *d.* more than the other, I demand how much each had, and what was their Father's Estate. *Answer*, The first had 673 *l.* 10 *s.* 9 *d.* and the second 1180 *l.* 12 *s.* 6 *d.* and their Fathers Estate was 2125 *l.* 2 *s.* 6 *d.*

A certain Person gave to one of his Children  $\frac{3}{4}$  of  $\frac{2}{5}$  of his Estate, and of the Remainder he gave another  $\frac{3}{8}$  of  $\frac{2}{3}$ , and when they told their Money, the one had 173 *l.* 12 *s.* 4 *d.* more than the other, How much had each, and what was their Father's Estate. *Answer*, the first had 416 *l.* 13 *s.* 7 *d.*  $\frac{1}{5}$ . The Second 243 *l.* 1 *s.* 3 *d.*  $\frac{1}{5}$ . And their Father's Estate was 3388 *l.* 18 *s.* 8 *d.*

---

---

THE  
DOCTRINE  
OF  
Decimal Fractions.

WHAT a Fraction is, and how read, I have already declared in the Doctrine of Vulgar Fractions, and therefore I shall here only shew the different way of Noting these from that of Vulgar, with their great use in the Solution of several Arithmetick Questions.

A *Decimal Fraction* is that which hath for its Denominator an Unite, with a certain Number of Cyphers as 10, 100, 1000, 10000, &c. are all Denominators of Decimal Fractions.

Hence 'tis evident, that we divide the Unite into 10, 100, 1000, 10000, &c. equal parts. For dividing it first into 10 equal parts, and each of those are again



again divided into 10 other equal parts; so that the Unite will then be divided into 100 equal parts; and if again we divide each of those hundred equal parts into ten other equal parts, the Unite or Integer will be divided into 1000 equal parts; And so by Decimating the first, and Subdecimating the second, we proceed *ad infinitum*.

Now because all the Denominators of Decimal Fractions differ only in the Number of places, and not in the Figures, they being always an Unite with Cyphers, they may be express'd without their Denominators with a point before them, as  $\frac{6}{10}$  is thus express'd .6, and  $\frac{54}{100}$  thus .54, also  $\frac{27}{1000}$  thus .027 And observe, that this point distinguishes them from whole Numbers.

Hence the Denominator of a Decimal Fraction is easily known by the places of the Numerator, the Denominator being always one place more, as .6 hath 10 for its Denominator, and .54 hath 100, and .027 hath 1000 for its Denominator, understand the like of any other.

The order of places in Decimals is from left to right, and therefore contrary to the order of places in a whole Number,

ber which is from right to left, as in this Decimal .548, here 5 is in the first place next the left hand, and signifies so many tenth parts of an Unite, and is therefore called *Primes* ; the 4 which is in the second place, signifies so many hundred parts of an Unite, and is called *Seconds* ; the figure 8 which possesses the third place from the left hand, denotes so many thousandth parts of an Unite, or Integer, and is called *Thirds*, and so on, as in the following Table.

*The Notation Table for Decimals.*

of Unity.					
Tenth parts	Hundr. parts	Thouf. parts	X Thouf. parts	C Thouf. parts	Mill. parts
.3	5	7	9	8	4
Primes	Seconds	Thirds	Fourths	Fifths	Sixths

This



This Table consists only of a Decimal Fraction, against which above is set the Value of each place, and below its Name.

From a little consideration of what has been said 'tis evident, that Cyphers prefix'd on the right hand of the Numerator of a Decimal Fraction, do neither increase nor lessen its value. For .2 is of the same value with .20 or .200 &c. And therefore 'tis very easy reducing Decimal Fractions to a common Denominator, for 'tis but setting Cyphers on the right hand of the Numerator: As suppose .3 and .84 and .476 and .2356 were Decimal Fractions, and it was required to reduce them to one Denominator; here I consider that the Denominator of the greatest Decimal given is 10000, I therefore add so many Cyphers to each of the Numerators that will make each of their Denominators to consist of five places, so that the above proposed Decimals, when reduced, stand thus .3000 and .8400 and .4760 and .2356.

I have been as clear as possible in explaining the Notation of these Numbers, because of the great facility they bring with their practice in several Operations,

not only in Arithmetick, but in most other parts of the Mathematicks. For, had our first Institution of Dividing our Money, Weight, Measure, &c. been Decimally, we had never been troubled with so many Fractions, which cause such great tediousness in several Operations. And indeed the Art of Arithmetick would be taught with much more ease and expedition than now it is, in case such a Reformation should ever be brought to pass.

### *Reduction of Decimals.*

**W**Hat is here to be done is no more than what was shown in *Reduction* the 5<sup>th</sup>. of Vulgar Fractions, only here I shall more largely comment upon what I there but hinted; and show in the first place how to reduce a Vulgar Fraction to a Decimal, and then how to find the Value of any Decimal in the known parts of Coin, Weight, Time, &c. and that with as much brevity and clearness as I can.



*To Reduce a Vulgar Fraction to a  
Decimal.*

**T**He proportion for reducing a Vulgar Fraction to a Decimal, is, *As the Denominator of the Vulgar Fraction to its Numerator, So is 10, 100, 1000, &c. or any assign'd Denominator, to its Numerator, that is to the Decimal required.*

*Exam. 1.* Suppose it was required to reduce  $\frac{3}{4}$  to a Decimal Fraction, the Operation is as follows,

As 4 to 3 so is 10000

$$\begin{array}{r}
 \begin{array}{r}
 4 \overline{) 30000} \text{ (7500} \\
 \underline{28} \dots \\
 20 \\
 \underline{20} \\
 .00
 \end{array}
 \qquad
 \begin{array}{r}
 \phantom{0000} 3 \\
 \hline
 30000 \\
 \hline
 \end{array}
 \end{array}$$

So that .7500 or .75 (for Cyphers on the right hand a Decimal Fraction neither increafes nor diminishes its value) is the Decimal equivalent to  $\frac{3}{4}$ .

*Note*

*Note.*

From the preceding proportion 'tis evident, That if to the Numerator of any Vulgar Fraction you annex so many Cyphers, as you would have your Decimal to consist of places, and divide by the Denominator, the Quote gives the Decimal required.

*Exam. 2.* Reduce  $\frac{15}{19}$  to a Decimal of five places.

To 15 the Numerator of the given Vulgar Fraction I annex five Cyphers, it makes 1500000, this I divide by 19 the Denominator, the Quote is the Decimal required. See the following Operation.

$$\begin{array}{r}
 19 \overline{) 1500000} \quad (78947 \\
 \underline{133} \phantom{0000} \\
 170 \phantom{000} \\
 \underline{152} \phantom{00} \\
 180 \phantom{0} \\
 \underline{171} \\
 90 \\
 \underline{76} \\
 140 \\
 \underline{133} \\
 7
 \end{array}$$

So



So that the Decimal equal to the given Vulgar Fraction is .78947, which because of the remainder, is not exactly the truth, yet 'tis so near, that it wants not  $\frac{1}{100000}$  part of an Unite of the truth, and if you proceed farther to make the Decimal consist of six places, it will be .789473, and then it will not want  $\frac{1}{1000000}$  part of an Unite of the truth; for if the Decimal be made .789474, it would exceed the true value.

And thus by Increasing the Number of places in the Decimal you may at last come infinitely near, tho' never to the truth it self.

*Exam. 3.* Reduce  $\frac{1}{32}$  into a Decimal of five places.

$$\begin{array}{r}
 32 \overline{) 100000} ( 3125 \\
 \underline{96 \dots} \\
 40 \\
 \underline{32} \\
 80 \\
 \underline{64} \\
 160 \\
 \underline{160} \\
 :
 \end{array}$$

Here

Here ( because the Decimal is required to five places ) I add five Cyphers to 1 the Numerator of the given Fraction, and then divide by 32 the Denominator, the Quote gives 3125 for the Decimal sought.

But here Note, that because I annex'd five Cyphers to 1 the given Numerator, and there arises but four figures in the Quote, I must supply such defect by prefixing as many Cyphers on the left hand of the first figure in the Quote as there wants places, as in the preceding Example. where the Quote consisted but of four figures or places, here I annex a Cypher on the left hand of 3 the first figure in the Quote, and then it becomes .03125 which is the true Decimal required.

*To Reduce the known parts of Money, Weight, Time, &c. to a Decimal Fraction.*

**F**ROM what precedes, 'tis evident how the known parts of Money, Weight, Time, &c. may be turn'd into a Decimal of the same Value, or Infinitely near it, for if in Money, a Pound Sterling be an Integer, whatsoever is less than



than a Pound, is either a part or parts of the same; and when you know what part or parts thereof it is, you may easily Reduce it to a Decimal of the same Value, from what was taught in the last.

*Exam.* What's the Decimal of 9 s. That is Reduce  $\frac{9}{20}$  into a Decimal consisting of two places.

$$\begin{array}{r} 20 \overline{) 900} \quad (45 \\ \underline{80} \\ 100 \\ \underline{100} \\ 000 \\ \underline{\phantom{000}} \end{array}$$

Here working according to what has been before directed, I find the Decimal of 9 s, to be .45

So if I would know the Decimal of 9 d. here I consider that 9 d. is  $\frac{9}{12}$  of  $\frac{1}{2}$  of a Pound or  $\frac{3}{4}$ .

Working therefore according to the preceding Rule, I find the equivalent Decimal to be .0375.

Again, if I would know the Decimal of 3 Farthings, here I must consider that 3 Farthings is the  $\frac{3}{4}$  of  $\frac{1}{2}$  of  $\frac{1}{2}$  or  $\frac{3}{16}$  of a pound, and therefore working as before, I find the Decimal to be .0031 near.

G

Lastly,

*Lastly*, if it were requir'd to find the Decimal of 7*l.* 08*s.*  $\frac{3}{4}$  that is 371 Farthings, or  $\frac{271}{1000}$  here repeating the like operation, I find the Equivalent Decimal to be 3864, the like is to be understood in reducing to Decimals, the known parts of Weight, Time, Measure, Motion, &c.

*To find the Value of a Decimal Fraction in the known parts of Money, Weight, Time, &c.*

**T**His is but the Converse of the former ; and therefore the Rule for finding the Value of a Decimal is grounded upon the same reason as that of turning any part of Coyne, &c. to a Decimal.

For 'twill hold *as the Decimal Denominator is to its Numerator, So is the parts in the next Inferior Denomination to the Numerator, or Number of such parts contain'd in the Decimal.*

And hence comes this Rule. Multiply the given Decimal by the parts of the next inferior Denomination, that are equal to the Integer the Decimal gives the parts of, and from the product cut  
of



of so many figures towards the right hand as there are places in the given Decimal, the remaining figures on the left side are the value of the said Decimal in the next inferior Denomination: If any thing remain, it is the Decimal of an Integer in the Denomination last found, and may be reduced as low as you please by the same Rule, and after the same manner, as it was in *Reduct. 5th.* of Vulgar Fractions.

*Exam.* How much is .3765 of a pound Sterling. I say,

As 10000 to 3765, So is 20 to 7 s. 6 d.

20

( $\frac{1}{4}$  44

10000) 75300

See the work.

6|3600

4

1|4400

So that from the preceding Work I find the true Value of this Decimal of a Pound sterling .3765 to be 7 s. 6 d.  $\frac{1}{4}$ .44 After a like process may the Value of any Decimal of Weight, Time, Measure, &c. be found.

Some more Examples, I might here have added, but I think the Method is so plain, that it will be needless ; I shall therefore forbear, and in the room thereof show you a brief, and practical Rule for finding the value of any Decimal of a Pound Sterling, as soon as ever you hear it nam'd,

*The Rule is*

The figure in the first place, or place of Primes, being doubled gives you the Number of Shillings, and if the Figure in the second place be 5, or above it, take one Shilling for the five, and add to the former Number of Shillings, found by doubling, then for that which remains above 5, with the Figure in the third place, count so many Farthings less by 1, that those two Figures make, being set in a Numeral Order, or if the Figure in the second place be under 5, then reckon so many Farthings wanting 1, as that and the Figure in the third place of the Decimal make in Number. An Example or two will make it plain.

*Exam. 1.* What's the .375 of a pound Sterling.

Here I double 3, which stands in the place of Primes, and that gives 6s. then  
because



because the next Figure (7) is above 5, I add one Shilling to the 6 before found, and it makes 7 s. then the 2 which is left of the 7, with the 5 in the place of thirds, makes 25, which being less'n'd by 1, gives 24 Farthings, so that the value of .375 is 7 s. 6 d.

*Exam. 2.*

What's the Decimal of .719.

Here the first figure 7 doubled gives 14 for the Number of Shillings, as before, and for the other 19 that remains I account 18 Farthings, which is  $4d \frac{1}{2}$ . so that the value of the Decimal .719 is 14 s.  $4d \frac{1}{2}$ .

More Examples might here be given, but I think these are sufficient to illustrate this practical way of finding the value of the Decimal of a pound Sterling.

I shall conclude this with the Insertion of the Decimal Table, for finding the value of any Decimal of a pound Sterling, omitting those of *Weight, Measure, Time, &c.* because of their being so seldom used, and if required, so easily Calculated from the aforementioned proportion, and likewise for their frequency in Books of this Nature.

*A TABLE, showing the Decimal of any part of a Pound sterling, & contra.*

Shillings.	19	.95	Pence.	11	.04584
	18	.9		10	.04166
	17	.85		9	.0375
	16	.8		8	.03333
	15	.75		7	.02917
	14	.7		6	.025
	13	.65		5	.02083
	12	.6		4	.01667
	11	.55		3	.0125
	10	.5		2	.0083
	9	.45		1	.00417
	8	.4	Farth.	3	.00312
	7	.35		2	.00208
	6	.3		1	.00104
	5	.25			
	4	.2			
	3	.15			
	2	.1			
	1	.05			

*The Use of the Table.*

The method of making this Table is evident from what precedes, and its use almost as apparent. Let the Decimal of 13 s. 7 d.  $\frac{1}{2}$ . be required, Seek in the Table first for the Decimal of 13 s. which is .65 next for the Decimal of 7 d. which is



is .02917, and lastly for the Decimal of  $\frac{1}{2}$ , which is .00208; I set these Decimals in the order following, and add them together.

$$\begin{array}{r}
 13 \text{ s. } 65 \\
 7 \text{ d. } 02917 \\
 2 \text{ q. } 00208 \\
 \hline
 13 \text{ s. } 7 \text{ d. } 2 \text{ q. } 68125
 \end{array}$$

By which you see the Decimal of 13 s. 7 d.  $\frac{1}{2}$  is .68125. In like manner may the Decimal of any other Sum be found, as also the Sum belonging to any given Decimal.

### *Addition of Decimals.*

**A**S to the manner of adding, 'tis the same as in common Addition, the business being only to see that they are rightly plac'd, according to the manner of their Notation, which thing is easily effected, by setting the point prefixt to them under each other; for then the rest of the places will fall right, whether they be whole Numbers and Decimals, or all Decimals.

*Some*

*Some Examples.*

	<i>pts</i>	<i>In. pts</i>	<i>In. pts</i>
	.427	2.43	27.67
	.3583	5.67	615.369
	.67526	4.38	2.19
	<hr/>	<hr/>	<hr/>
Sum	1.46056	12.48	645.229
	<hr/>	<hr/>	<hr/>

Here you see in all these cases that Primes stands under Primes, Seconds under Seconds, &c. And where Integers are joyn'd with Decimals, there unites, stands under unites, and Tens under Tens, &c. In which Examples 'tis very plain, that the method of adding is put as it was in whole Numbers, only here you are to make the summ consist of no more Decimal places, then is in the greatest part of it. As in our first Example, the Summ consisted of six places or Figures, and the greatest part but of five, I therefore cut off five Figures in the Sum, toward the right hand for the Decimal parts, the remainder on the left are Integers.

*Note,* That in this, and the following Rule, the Decimals given to be added, or  
Sub-



Subtracted, must be parts of the same whole.

*More Examples,*

What's the Sume of 29 & 3.007 & .94 & 89.76. *Answer.*

What's the Sume of 3.87 & 486 & .4 & .025. *Answer.*

What's the Sume of 59.4 & 8.796 & 472.6 & .142. *Answer.*

*Note,* that *In.* over the preceding and following Sums stands for *Integer*, and *pts.* for *Parts*.

---

*Substraction of Decimals.*

**T**He Operation here is in all respects like to that in Vulgar Substraction, the main thing ( as in the last ) being only to see that they are rightly placed, which is done by the direction given in the foregoing Rule of Addition.

*Some Examples*

$\begin{array}{r} .456 \\ .287 \\ \hline \end{array}$	$\begin{array}{r} 2.352 \\ .87 \\ \hline \end{array}$	$\begin{array}{r} 58.1 \\ .296 \\ \hline \end{array}$
Rema. $\begin{array}{r} .169 \\ \hline \end{array}$	$\begin{array}{r} 1.482 \\ \hline \end{array}$	$\begin{array}{r} 57.804 \\ \hline \end{array}$

Here you see we Subtract as in common Subtraction, only observe, that where the Decimals have not an equal Number of places, the vacancies are supplied with Ciphers, or are understood so to be, especially in the upper Number.

*More Examples.*

From 15 subtract 7.8 *Answ.* 7.2  
 From 1 subtract .9872 *Answ.* .0128  
 From 58.6 subtract 3.98625. *Answ.*  
 54.61375

---

*Multiplication of Decimals.*

**I**N Multiplication of Decimals, both the manner of placing and multiplying is in all respects and cases, the same with that of placing and multiplying whole Numbers, the business here being only



only to find the value of the Product after the Operation is ended, which to do take this general

*Rule.*

*See how many Decimal places there are in the Multiplicand and Multiplier, and from the Product toward the right hand cut off so many as are in both these, so shall the Figures on the right hand of the point be Decimal places, and those on the left side Integers.*

5.46	21,67	.67.23
14	2.3	.63
<hr/>	<hr/>	<hr/>
2184	6531	020169
546	4334	40338
<hr/>	<hr/>	<hr/>
Prod. 7644	49.841	.423549
<hr/>	<hr/>	<hr/>

But if when the Multiplication is ended, there arise not so many Figures in the Product, as ought to be cut off, then is such defect to be supply'd, by annexing as many Cyphers on the Left Hand thereof, as there wants places; with a point before them, and you have the true value of the product; See the following *Examples.*

H 2

.158

	.158		.227
	.6		.02
	<hr/>		<hr/>
Prod.	948		454
True Prod.	0948		.0454
	<hr/>		<hr/>

The consideration of this practice will be of some help to you, in finding the true value of the Quote in Division.

*More Examples.*

Mult.	4000000	.0000001	232
By	.0000003	900	438
	<hr/>	<hr/>	<hr/>
Prod.	1.2000000	.000900	101.616
	<hr/>	<hr/>	<hr/>

*Of Contraction in Multiplication of mixt Numbers.*

**T** Here is in this kind of Multiplication, a certain way of Contraction, by which you may get the product, to as few, or many places as you please, without the tedious Multiplication of the whole; the Method of which is as follows.

As Suppose 9.58 was to be Multiplied by 8.79, here 'tis evident the decimal will



will consist of 4 places, and only two would be sufficient.

Set down the bigger of the two Quantities for the Multiplicand, and then set the place of Unites in the Multiplier, under that place of parts in the Multiplicand, you would have in the product, and then invert the Order of all the other places in the Multiplier, *that is*, set the place of Tens, where Primes should be, and the place of Primes where Tens should be, and so on with the inversion of the rest; then let each Figure of the Multiplier, Multiply that of the Multiplicand, which is just over, Remembring to add, what would have been brought thither from the following places; then add up all together, and from the Sum cut off two Figures (in this Example) next the Right Hand, and you have your desire, all which by the following Examples, compar'd with this direction will plainly appear.

*Exam-*

*Example 1st.*

By the common way      By Contraction

9.58	Multiplicand	9.58
8.79	Multiplior	97.8
<hr/>		<hr/>
84.2082		7664
		670
		86
		<hr/>
	Prod.	84.20
		<hr/>

*Example 2d.*

By the Common way      By Contraction

342.6894	Multiplicand	3426894
52.678	Multiplior	876.25
<hr/>		<hr/>
18052.1922132		17134470
<hr/>		685378
		205613
		23988
		2741
		<hr/>
	Prod.	18052.190
		<hr/>

This last was requir'd to three places,  
where you see they are seperated by a  
point



point toward the Right Hand, being 190, but should have been 192; which small Errour is caus'd by the want of the Carriage from the next row, and therefore if you would have it exactly to 3 places, especially in great Summs, you ought to do it to four.

---

### *Division of Decimals.*

**T**HE manner of working Decimal Division, is in every thing like to that of Common Division, and therefore no regard as to their place and Nature is here to be had, any more than what was in Division of whole Numbers; the Mystery of this lying first in their preparation, when need requires. *Secondly*, In finding the true Value of that Quote after the Division is ended.

*First*, Therefore when it happens, that the Divisor has more places than the Dividend, you must put to the Right Hand of the dividend, (whether it be a whole Number, mixt or Decimal Fraction) a certain Number of Ciphers at pleasure, by which it is made fit for Operation.

As

As suppose 14<sup>1</sup> was to be divided by 361, 'tis evident here is an absolute Necessity of prefixing Ciphers to 14 the Dividend, before you can divide by 361 the Divisor.

The Dividend being thus prepared take Notice, that there must be as many decimal places in the Divisor and Quotient as are in the Dividend; for the dividend is in effect the product, and the Divisor and Quotient the Multiplicand and Multiplier. And therefore for the finding the value of the Quotient this is the

*Rule.*

*Look how many Decimal places are in the Dividend, more than in the Divisor, for so many Decimal places will there be in the Quotient.*

And here Note, that you must be sure to make the Dividend consist of more places than the Divisor, if it doth not so already, which is easily done, by adding Ciphers.

*Exam-*



*Example.*

$$.56 ) 24 ($$

$$83 ) .35 ($$

$  \begin{array}{r}  56 \overline{) 24.0000} (4285 \\  \underline{224} \phantom{000} \\  160 \phantom{00} \\  \underline{112} \phantom{00} \\  480 \phantom{00} \\  \underline{448} \phantom{00} \\  320 \phantom{00} \\  \underline{280} \phantom{00} \\  40 \phantom{00} \\  \underline{\phantom{00}}  \end{array}  $	$  \begin{array}{r}  83 \overline{) 350000} (4216 \\  \underline{332} \phantom{000} \\  180 \phantom{00} \\  \underline{166} \phantom{00} \\  140 \phantom{00} \\  \underline{83} \phantom{00} \\  570 \phantom{00} \\  \underline{498} \phantom{00} \\  82 \phantom{00} \\  \underline{\phantom{00}}  \end{array}  $
---	---

Having annexed 4 Ciphers to each of the Dividends, the first Dividend being an Integer, consists only of the 4 Decimals added; but the later being a Decimal, is made to consist of six Decimals by the 4 Ciphers that was added; they being thus prepared, and the work of Division over, you see the Quote consists; of 4 places; now considering how many

I                      Decimal

Decimal places there is in each of those Quotes more than in their proper Dividends, and you shall find that in the first Quote, there ought to be two places of Decimals, and in the second six of the like places, which because there is but four, I prefix two Ciphers on the Left Hand thereof, which makes it .004216.

*Some more Examples.*

84)3.5(    54)1.5(    .9).004(    .63)1(

prepar'd 3.50000

true Quote .04166

prepar'd .004000

true Quote .00444

prepar'd 1.50000

true Quote .2777

prepar'd 10000

true Quote .158

I have to these 4 Examples, set only the Dividends prepar'd with their Quotients truly Valued, the consideration of which, with the preceding direction, I hope will be a sufficient light in all other Cases that can happen.



*Of the Use of Decimals.*

**T**O show the use of these Numbers in all Solutions, where they might be applied in Expediting an Operation, would be endless, they being of great use in most parts of the Mathematicks; but particularly, and principally in Gauging, Surveying, and Measuring, Calculating the Tables of Interest, raising of Logarithmes; as may be seen in most Books, that have Writ of these Subjects, I shall therefore forbear giving Examples of using them in any of these parts, Except I had Treated distinctly of each of them; and shall close this Paragraph with the Collection of a few easy Questions, which are very speedily and easy solv'd by these Numbers.

*By Multiplication.*

**I**N 756 Pistoles, at 18 s. each, How many Pounds Sterling. *Answ.* 680 l. 08 s.

In 439 Guinea's, at 22 s. 6 d. each, How many Pounds sterling. *Answ.* 493 l. 17 s. 6 d.

If I spend 4 s. 6 d. per Day, How much is that for one Year. *Answ.* 82 l. 2 s. 6 d.

If a yard of Cloth is worth 6 s. 9 d. What comes 59 Yards to at that Rate. *Answ.* 19 l. 18 s. 3 d.

If a piece of Paving be 34 foot, 6 inches long, and 24 foot, 9 inches broad, What's the Content in square feet. *Answ.* 853 foot .875

If one Man's share in the Cargo of a ship come to 38 l. 14 s. What was the whole worth, supposing there was 158 Men in the ship. *Answ.* 6114 l. 12 s.

If the Interest of 500 l. for one Day is 2 s. 3 d. What's that for a Year. *Answ.* 41 l. 1 s. 3 d.

### By Division.

**I**N 680 l. 8 s. How many Pistoles, at 18 s. each. *Answ.* 756.

In 493 l. 17 s. 6 d. How many Guinea's at 22 s. each. *Answ.* 439.

If I spend 82 l. 2 s. 6 d. in one year. What is that for one day. *Answ.* 4 s. 6 d.

If 59 Yards of Cloth cost 19 l. 18 s. 3 d. What Cost one Yard. *Answ.* 6 s. 9 d.

If



If the Content of a piece of Paving be 853 Foot .875 and the length be 34 foot 6 Inches. What's the true breadth. *Answ.* 24 Foot 9 Inches.

If the whole Cargo of a ship be 6114 *l.* 12 *s.* and there be 158 men in the ship. What comes each man's share. *Answ.* 38 *l.* 14 *s.*

If the Interest of 500 *l.* for a Year is 41 *l.* 1 *s.* 3 *d.* What is that for one day. *Answ.* 2 *s.* 3 *d.*

I conceive it needless to meddle with the Rule of Three, it being in all kinds and respects performed like that in Vulgar Fractions; I shall therefore leave the Exercise of Questions of this nature to the Ingenious.

---

*A Specimen of the Demonstration of the Operations of Vulgar and Decimal Fractions.*

**I** Shall first begin with that of Vulgar Fractions, and in order to the more clear apprehending thereof, I must make a short Repetition of what has been already declared in the first page, *viz.*

That

That a Fraction is a part or parts of some divisible Integer, and is represented by two Numbers, the one above the other beneath a Line thus  $\frac{2}{5}$ .

The Number placed beneath the Line is called the Denominator, and shows what parts the Unite is divided into.

The Number placed above the Line is called the Numerator, and shows how many of those parts are to be taken in the Fraction.

As the Fraction  $\frac{2}{5}$  denotes two such parts as the Integer contains 5.

From this method of expressing Fractions it follows.

That every Fraction is to its whole an Unite, as the Numerator is to the Denominator, and consequently.

*First*, That if the Numerator be  $\begin{cases} \text{greater} \\ \text{equal} \\ \text{less} \end{cases}$  than the Denominator, the Fraction is accordingly greater equal or less than its whole an Unite. The first and second of these kinds are called Improper Fractions, the last are termed Proper.

*Secondly*, That Fractions are not to be estimated by the greatness of their Numbers by which they are express'd, but by the proportion the Numerators bear to the Denominators.

*Thirdly*,



*Thirdly*, That Fractions, whose Numerators to their Denominators bear the same proportion, are equal as  $\frac{1}{2} \cdot \frac{3}{6} \cdot \frac{10}{20}$ .

*Fourthly*, That every Fraction is the Quotient of the Numerator divided by the Denominator.

This being granted, I propose the following *Lemma*.

*Lemma.*

*If a Number multiply two Numbers, their Products are in such proportion to each other, as the Numbers multiplied are to themselves.*

For 3 multiplying  $\left\{ \begin{smallmatrix} 6 \\ 8 \end{smallmatrix} \right\}$  produceth  $\left\{ \begin{smallmatrix} 18 \\ 24 \end{smallmatrix} \right\}$  then I say that  $6 : 8 :: 18 : 24$ . Which thing is evident from the common Notion of Multiplication. For  $1 : 3 :: \left\{ \begin{smallmatrix} 6 : 18 \\ 8 : 24 \end{smallmatrix} \right\}$  and therefore  $6 : 18 :: 8 : 24$  by the 11th. of the Fifth of *Euclid*.

But by *alternation*  $6 : 8 :: 18 : 24$ , which was to be proved.

Having laid down this as a foundation, I shall proceed to a Demonstration of each particular Operation.

*Re-*

*Reduction the First.*

This is so clear from the nature and manner of expressing a Fraction, as also from the first consequent, that it needs no farther Demonstration.

*Reduction the Second.*

The Proof of this is a consequent from that of Multiplication, and therefore I refer it to that place.

*Reduction the Third.*

This teaches to abbreviate a Fraction, by dividing both Numerator and Denominator by any Number that will divide both without a remainder.

As suppose  $\frac{6}{8}$  is given to be reduced to its lowest Terms, here dividing 6 by 2, and 8 by 2, there arises  $\frac{3}{4}$ ; now since 3 and 4 multiplied by 2 produces the same Numbers, viz.  $\frac{6}{8}$ . therefore  $3 : 4 :: 6 : 8$  and therefore the Fraction  $\frac{3}{4}$  is equal to  $\frac{6}{8}$  by the *Lemma*, and third Consequent.



*Reduction the Fourth.*

This teaches to reduce Fractions of divers Denominations into one Denomination, having the same value, for doing of which the

*Rule is*

Multiply all the Denominators for a common Denominator, then multiply each Numerator into all the Denominators, except its own, for a new Numerator.

As suppose  $\frac{3}{8}$  and  $\frac{2}{7}$  were given to be so reduced.

From the Operation according to the Rule they will stand thus  $\frac{3 \times 7}{8 \times 7}$  and  $\frac{8 \times 2}{8 \times 7}$  that is  $\frac{21}{56}$  and  $\frac{16}{56}$ , which Fractions are by the aforefaid *Lemma* and third Consequent equal to those given.

Again, Suppose  $\frac{2}{3} \cdot \frac{3}{4} \cdot \frac{4}{5}$  were given thus to be reduced. The Fractions  $\frac{2 \times 4 \times 5}{3 \times 4 \times 5} \cdot \frac{3 \times 3 \times 5}{3 \times 4 \times 5} \cdot \frac{3 \times 4 \times 4}{3 \times 4 \times 5}$  that is  $\frac{40}{60} \cdot \frac{45}{60} \cdot \frac{48}{60}$  are evidently equal to the Fractions proposed by the said *Lemma*, and third Consequent.

*Reduction the Fifth.*

This is proved in the Reduction of a Vulgar Fraction to a Decimal.

*Of Addition and Substraction of Fractions.*

**T**He Fractions whose Summ or Difference is required must be reduced to equal Fractions, having the same Denomination. And then according to the Rule the  $\left\{ \begin{array}{c} \text{Summ} \\ \text{Difference} \end{array} \right\}$  of the Numerators placed over the common Denominator is the  $\left\{ \begin{array}{c} \text{Summ} \\ \text{Difference} \end{array} \right\}$  of the Fractions requir'd.

*Exam.* What's the Summ and Difference of  $\frac{3}{8}$  and  $\frac{2}{7}$ .

The Fractions reduced to others equal to them, and of the same Denomination are  $\frac{21}{56}$  and  $\frac{16}{56}$  consequently  $\frac{21 \pm 16}{56}$  is

the  $\left\{ \begin{array}{c} \text{Summ} \\ \text{Difference} \end{array} \right\}$  of the Fractions, that is the Summ is  $\frac{37}{56}$ , the Difference  $\frac{5}{56}$ , which was required.

*Of Multiplication of Fractions.*

For finding the product of any two Fractions, this is the

*Rule.*



*Rule.*

Multiply the Numerators together for a new Numerator, and the Denominators together for a new Denominator, the Fraction thus produced is the product.

*Exam.* Suppose  $\frac{3}{4}$  was given to be Multiplied by  $\frac{2}{3}$ , the Product is

$$\frac{2 \times 3}{3 \times 4} = \frac{6}{12} = \frac{1}{2}.$$

The reason of which is evident, for by the 4<sup>th</sup>. Consequent I consider these Fractions as the Quotients of their respective Numerators divided by their Denominators, and so if I multiply  $\frac{3}{4}$  by 2 it gives  $\frac{2 \times 3}{4}$  for to double any Quotient, is to

<sup>4</sup>double the Dividend: But now since I have multiplied by 2, when I ought to have multiplied by  $\frac{1}{3}$  of 2, therefore  $\frac{1}{3}$  of this product is the truth, which I effect by tripling the divisor 4, Therefore  $\frac{2 \times 3}{3 \times 4} (= \frac{1}{2})$  is the product of  $\frac{2}{3}$  by  $\frac{3}{4}$ .

And here you may take notice, that the product of any Quantity multiplied by a Fraction is always less than the Quantity so multiplied.

The reason of which follows from the Principle of Common Multiplication, which is, that every Product contains the Dividend so often as the Divisor contains 1 or Unity. If therefore the Multiplier be less than 1 or Unity, the Product will be less than the Multiplicand; For according to this Principle, the Product must not contain the Multiplicand once, because the Multiplier doth not Unity.

Hence the Product of two Fractions is evidently less than either of them.

And hence also the reason of reducing Compound Fractions, to Simple ones is very clear; for to take the  $\frac{2}{3}$  of  $\frac{3}{4}$ , is no more than to Multiply those two Fractions together.

### *Of Division.*

For working of Division the  
*Rule is*

Multiply the Denominator of the Divisor into the Numerator of the Dividend for a new Numerator, and the Numerator of the Divisor into the Denominator of the Dividend for a new Denominator, the Fraction thus formed shall be the Quotient.

Suppose



Suppose  $\frac{2}{3}$  to be divided by  $\frac{3}{4}$ .

$$\frac{3}{4}) \frac{2}{3} \left( \frac{4 \times 2}{3 \times 3} \right) = \frac{8}{9} \text{ the Quotient.}$$

Here, as before, I consider the Fractions as Quotients : So that if the Example had been, How many  $\frac{1}{4}$  is in  $\frac{2}{3}$ ; the Answer would be  $\frac{4 \times 2}{3}$ , for that is only Quadrupling the Numerator. But since my Divisor is  $\frac{3}{4}$ , 'tis evident the former Quote is 3 times too much ; wherefore I take  $\frac{1}{3}$  of it by tripling the Divisor, and then it stands as above.

---

### *Of Decimal Fractions.*

**D**ECIMAL Fractions ( as I have elsewhere noted ) are only Fractions, whose Denominators are an Unite with Cyphers, as 10, 100, 1000, &c. And are conveniently written without their Denominators ; for if the Numerators consists of places equal in Number to the Cyphers in the Denominator, then prefix a point before the Numerator, and omit

omit the Denominator ; but if the Denominator do not consist of as many places as there are Cyphers in the Denominator, then you must supply that defect by putting Cyphers before the significant figures of such Numerator, with a point on the left hand of such Cypher, or Cyphers,

As  $\frac{3}{10}$   $\frac{78}{100}$   $\frac{86}{1000}$   $\frac{54}{10000}$  are

thus express'd .3 .78 .086. .0054

*To reduce a Vulgar Fraction to a Decimal.*

SAY, As the Denominator of the Fraction proposed, is to its Numerator, so is 10, 100, 1000 &c. that is, an Unite with as many Cyphers as I intend my Decimal shall have places, to the Numerator of a Decimal equal to it.

*Exam.*



*Example.*

Reduce  $\frac{3}{4}$  into a Decimal of two places

$$4 : 3 :: 100$$

$$\underline{3}$$

$$4 \overline{) 300} (75$$

$$\underline{20}$$

$$.$$

So that  $\frac{75}{100}$  or .75 is equal to the Fraction proposed by the third Consequent.

The 5th. Reduction is here prov'd, this being the same with that, only then we knew not the name of Decimals, for such Fractions as had 10, 100 &c. for the Denominator.

*Theorem.*

The Decimal Fraction .234 is equal to  $\frac{2}{10} + \frac{3}{100} + \frac{4}{1000}$  Also the mixt Quantity 3.856 is equal to  $8 + \frac{8}{10} + \frac{5}{100} + \frac{6}{1000}$ .

For

For  $\frac{2}{10} = \frac{200}{1000}$  &  $\frac{3}{100} = \frac{30}{1000}$  &  $\frac{4}{1000} = \frac{4}{1000}$  As also  $3 = \frac{3000}{1000}$  &  $\frac{8}{10} = \frac{800}{1000}$  &  $\frac{5}{100} = \frac{500}{1000}$  &  $\frac{6}{1000} = \frac{6}{1000}$ . But  $\frac{200}{1000} + \frac{30}{1000} + \frac{4}{1000} =$  the Summ  $\frac{234}{1000} = .234$  Also  $\frac{3000}{1000} + \frac{800}{1000} + \frac{500}{1000} + \frac{6}{1000} =$  the Summ  $3. \frac{856}{1000} = 3.856$  by the third Consequent.

Hence the first place after the Point in Decimals is the place of Tenths, the second of Hundredths, the third of Thousandths, &c. decreasing in a Subdecuple proportion, from Unity towards the right hand, as whole Numbers increase from Unity towards the left in a Decuple proportion. *Hence 'tis easie*

### *To Add or Subtract Decimals.*

#### *The Rule.*

Place Unites under Unites, Tenths under Tenths, Hundredths under Hundredths, &c. Then add or subtract, as if they were whole Numbers.

*Exam.*



*Exam. in Add.*

6. 4		6. 400	
298. 23	that is	298. 230	
43. 171		43. 171	
<hr style="border: 0.5px solid black;"/>		<hr style="border: 0.5px solid black;"/>	
347. 801	Sum	347. 801	Sum
<hr style="border: 0.5px solid black;"/>		<hr style="border: 0.5px solid black;"/>	

*Exam. in Sub.*

From 5. 46		From 5. 46	
Take 2. 9	that is	Take 2. 90	
<hr style="border: 0.5px solid black;"/>		<hr style="border: 0.5px solid black;"/>	
2. 56	remaind.	2. 56	rem.
<hr style="border: 0.5px solid black;"/>		<hr style="border: 0.5px solid black;"/>	

*Multiplication of Decimals.*

**M**ultiply Integers and Decimals together, as if all were Integers, and then cut off as many places from the Product towards your right hand, or Decimals, as is the Number of Decimal places in both Multiplicand and Multiplier.

**L***Exam.*

*Example.*

Multiply 32.4	.0023
by 7.6	.09
<hr style="width: 100px; border: 0.5px solid black;"/>	<hr style="width: 100px; border: 0.5px solid black;"/>
1944	Prod. .000207
2268	
<hr style="width: 100px; border: 0.5px solid black;"/>	
Prod. 246.24	
<hr style="width: 100px; border: 0.5px solid black;"/>	

Here 32.5 is  $\frac{325}{10}$  and 7.6 is  $\frac{76}{10}$ , which two Fractions multiplied by the Rule given for Multiplication of Vulgar Fractions produce  $\frac{24624}{100}$  or 246.24 The same holds in all other.

### *Division of Decimals.*

**D**ivide the Dividend by the Divisor in all respects, as in whole Numbers, only observe that so many Decimal places as there are in the Dividend more than there are in the Divisor, so many must be cut off from the Quotient to the right hand for Decimals.

*Exam.*



*Example.*

Divide 7.9 by 34.3

$$\begin{array}{r}
 34.3 \ ) \ 7.9000 \ (.230 \\
 \underline{686} \ \cdot \cdot \cdot \quad \underline{\hspace{1cm}} \\
 1040 \\
 \underline{1029} \\
 119
 \end{array}$$

For  $34.3 = \frac{343}{10}$  &  $7.9 = \frac{79}{10} = \frac{790000}{100000}$ .

$\frac{343}{10} ) \frac{790000}{100000} ( \frac{790000}{3430000} = ,200 \text{ near.}$

The reason of which is evident from  
Division of Vulgar Fractions.

*F I N I S.**Advertisement.*

**A**LL Sorts of Mathematick Instruments both for Sea and Land, are most Correctly Made, and Sold, by *John Worgan*, under *St. Dunstan's Church* in *Fleetstreet*.